

Fake Moustache and Glasses – Full Solution Guide

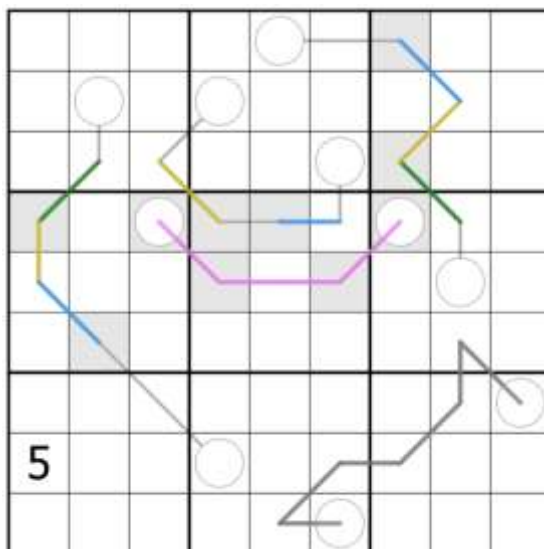
This is a full solution guide to my puzzle *Fake Moustache and Glasses*, and so spoilers are ahead.

Rules

- Normal sudoku rules apply: Place the digits 1 to 9 once each in every row, column, and 3x3 box
- **Double Arrows:** Digits along a grey line sum to the same as the sum of the two connected circles
- In addition, each of the following constraints applies to exactly one double arrow in the grid, including its circles:
 - *Entropic:* A run of 3 digits must contain one low (1, 2, 3), one medium (4, 5, 6), and one high (7, 8, 9) digit
 - *German Whisper:* Adjacent digits differ by at least 5
 - *Modular:* A run of 3 digits must all contain different remainders when divided by 3, i.e. one from (1, 4, 7), one from (2, 5, 8), and one from (3, 6, 9)
 - *Palindrome:* Digits read the same forwards and backwards
 - *Renban:* Contains a non-repeating set of consecutive digits in any order

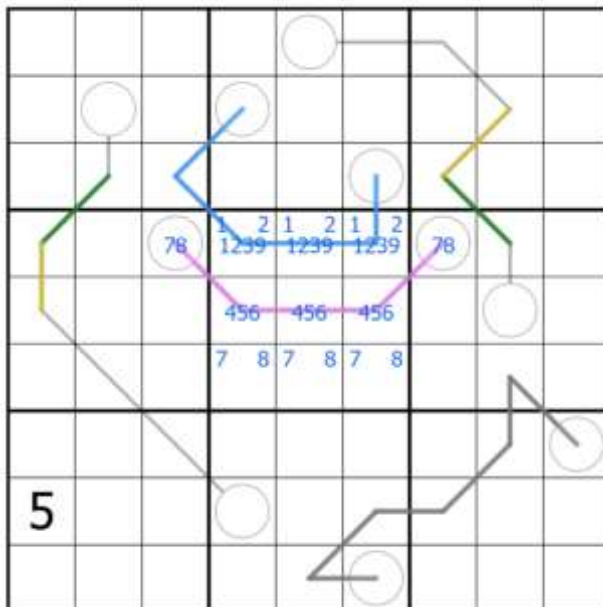
Solve Path

- One double arrow is a palindrome, and all of them have cells which see each other except for the double arrow covering R9C6
- One of the double arrows is a renban. Considering the possibilities, a 6 cell line that is a renban would have an odd total (e.g. 1-6 summing to 21) which could not be split into a 2/4 set to make a valid double arrow. A 7-cell set can't be split into a 5/2 set with the same sum. Hence the only 5 cell line must be the renban
- We can also rule out the line from R2C4 from being a German Whisper by available digits

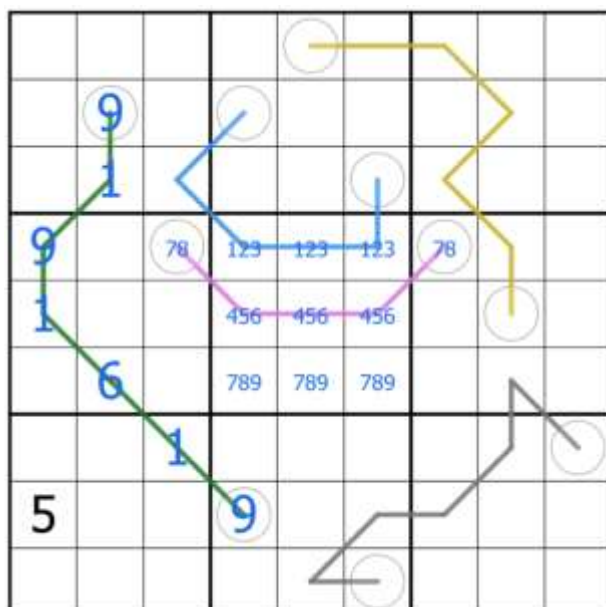


- The renban must have a set of digits which sum to an even number, which can only be 2-6 or 4-8. These would be split as $46 = 235$ or $78 = 456$
- Either of these options uses all of 456, so the line covering R4C456 is not entropic

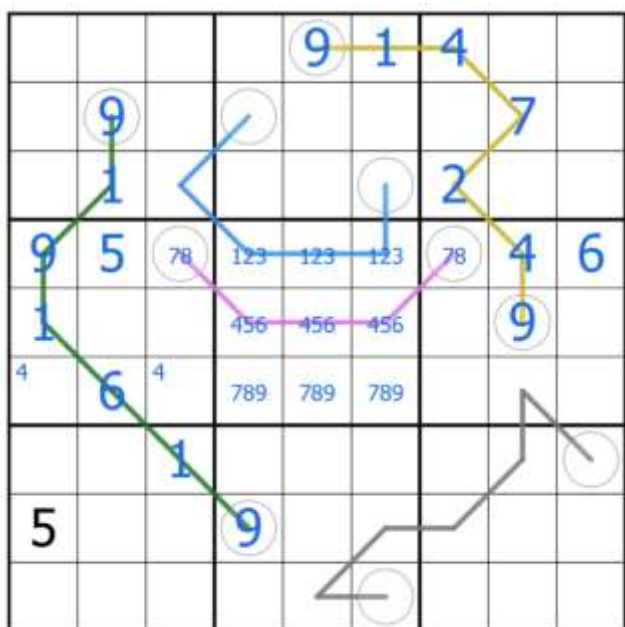
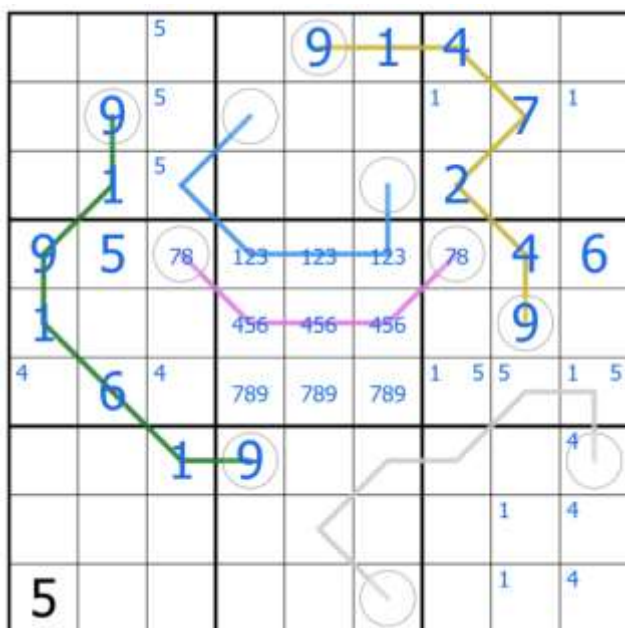
- If the renban were $46 = 235$ this only leaves 1789 to go on the line in $R4C456$, and there is no way to validly satisfy a double arrow and modular line with these digits available, hence the renban is $78 = 456$
- By renban logic we can also roughly place 78 in box 5



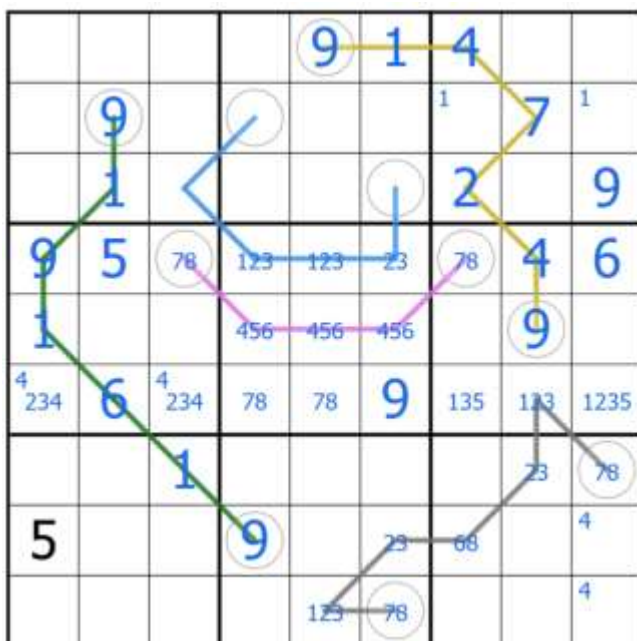
- 1 and 2 look at $R4C8$. If the $R5C8$ line were a German Whisper then the digits on the line would be minimum 38161 which sums to 19, hence this must be entropic, and the line at $R2C2$ is the German Whisper
- By the pointing 78 s, the line at $R2C2$ is completely forced to be $19161 = 9+9$
- Gives 123 triple in $R4$, 789 triple in $R6$



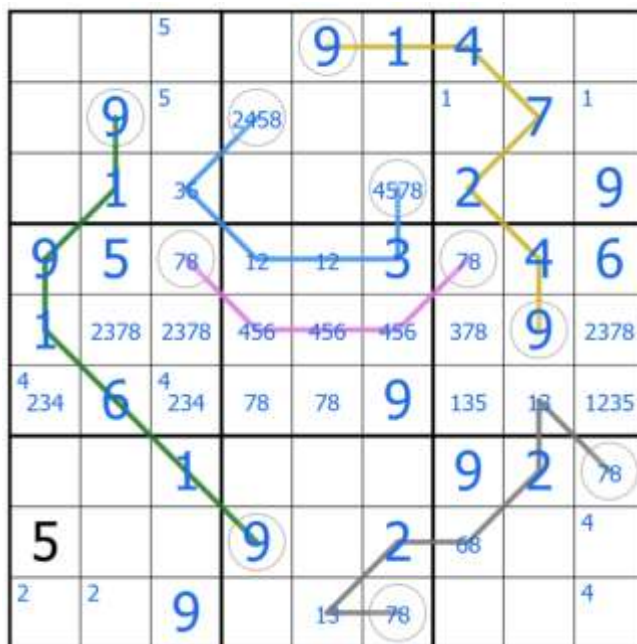
- Entropic line can only have one high digit which must be in $R2C8$
- 123 triple tells us that $R4C8$ is a medium digit
- 1 looking at $R3C7$ eats up our one degree of freedom and forces $42741 = 9+9$



- Centre digit of the palindrome must be an even digit, and sees 2 and 4. The end points also see 6 and 9, reducing the options
- Considering options for the other palindrome digits, $R6C8 + R7C8$ sum to no more than 6, giving a 23 pair in C6



- By modulo arithmetic the end points of the modular line are not from the 369 set, hence R4C6 is a 3 and R3C3 is from 36
- Places 2 on the palindrome



- R9C5 in box 9 is R8C9, and in box 3 is R2C7
- Considering the palindrome, we have either $7+7 = 1+2+8+2+1$, or $8+8 = 3+2+6+2+3$, either way 8 in box 9 is in either R7C9 or R8C7
- Creates a 135 triple in box 9, and a 678 triple in column 7

		5		9	1	4	6	
	9	5	2458			1	13	7
	1	36			4578	2	6	9
9	5	78	12	12	3	78	4	6
1	2378	2378	456	456	456	378	9	2378
4	234	6	4	234	78	78	9	135
		1				9	2	78
5			9		2	6	8	135
2	2	9		15	78	6	67	135
								4

- 3 is placed in column 7, then 5, 2 in box 6, and the palindrome is resolved

		5		9	1	4	68	35
	9	5	2458			1	7	35
	1	36			4578	2	68	9
9	5	78	12	12	3	78	4	6
1	278	278	456	456	456	3	9	78
34	6	34	78	78	9	5	1	2
		1				9	2	78
5			9		2	6	8	35
2	2	9		1	78	6	67	35
								4

- 1 is placed on the modular line, which makes R3C6 a 4 and reduce the remaining digits

		5		9	1	4	68	35
	9	5	58		568	1	7	35
	1	36			4	2	68	9
9	5	8	1	2	3	7	4	6
1	27	27	456	456	56	3	9	78
34	6	34	78	78	9	5	1	2
		1			568	9	2	7
5			9		2	8	3	1
2	2	9		1	7	6	5	4

- 5s are pencilmarked in box 1 and 3, so 5 in row 3 is in box 2, making R2C4 an 8
- Remainder resolves via sudoku

7	8	5	2	9	1	4	6	3
2	9	4	8	3	6	1	7	5
3	1	6	5	7	4	2	8	9
9	5	8	1	2	3	7	4	6
1	7	2	6	4	5	3	9	8
4	6	3	7	8	9	5	1	2
6	3	1	4	5	8	9	2	7
5	4	7	9	6	2	8	3	1
8	2	9	3	1	7	6	5	4